



SUB-OPTIMAL JOIN ORDER IDENTIFICATION WITH L1-ERROR

Yesdaulet Izenov², Asoke Datta¹, Brian Tsan¹ and Florin Rusu¹

¹Dept. CSE, University of California, Merced, CA, USA

²Dept. CS, Nazarbayev University, Astana, Kazakhstan



article



code



Q-error – the standard metric for quantifying the error of individual cardinality estimates – has been widely adopted as a surrogate for query plan optimality in recent work on learning-based cardinality estimation. However, the only result connecting Q-error with plan optimality is an upper-bound on the cost of the worst possible query plan computed from a set of cardinality estimates – there is no connection between Q-error and the real plans generated by standard query optimizers. Therefore, to identify sub-optimal query plans, we propose a learning-based method having as its main feature a novel measure called **L1-error**. Similar to Q-error, L1-error requires complete knowledge of true cardinalities and estimates for all the sub-plans of a query plan. Unlike Q-error, which considers the estimates independently, L1-error is defined as a permutation distance between true cardinalities and estimates for all the sub-plans having the same number of joins. Moreover, L1-error takes into account errors relative to the magnitude of their cardinalities and gives larger weight to small multi-way joins. Our experimental results confirm that, when L1-error is integrated into a standard decision tree classifier, it leads to the accurate identification of sub-optimal plans across four different benchmarks. This accuracy can be further improved by combining L1-error with Q-error into a composite feature that can be computed without overhead.

1 Problem

Can we classify the sub-optimality of a query plan based on true and estimated cardinalities?

| 2-way joins (CARDINALITY only) | | | | | |
|--------------------------------|-----------------|----------------|----------------|----------------|-----------------|
| index ρ | 1 | 2 | 3 | 4 | 5 |
| sub-plan | $cn \bowtie mc$ | $k \bowtie mk$ | $mc \bowtie t$ | $mk \bowtie t$ | $mc \bowtie mk$ |
| true Y | 388 | 41.8K | 2.6M | 4.5M | 34.9M |
| est. \hat{Y} | 973 | 20 | 1.5M | 2.7M | 13.8M |
| Q-error q | 2.51 | 2,092 | 1.70 | 1.70 | 2.53 |

| 3-way joins (CARDINALITY only) | | | | | |
|--------------------------------|---------------------------|----------------------------|--------------------------|---------------------------|---------------------------|
| index ρ | 1 | 2 | 3 | 4 | 5 |
| sub-plan | $cn \bowtie mc \bowtie t$ | $cn \bowtie mc \bowtie mk$ | $k \bowtie mk \bowtie t$ | $k \bowtie mk \bowtie mc$ | $mc \bowtie t \bowtie mk$ |
| true Y | 388 | 1,588 | 41.8K | 148.6K | 34.9M |
| est. \hat{Y} | 973 | 8,739 | 20 | 104 | 2.7M |
| Q-error q | 2.51 | 5.50 | 2,092 | 1,428.38 | 12.69 |

| 4-way joins (CARDINALITY only) | | | |
|--------------------------------|---------------------------|---------------------------|---------------------------|
| index ρ | 1 | 2 | 3 |
| sub-plan | $cn \bowtie mc \bowtie k$ | $cn \bowtie mc \bowtie t$ | $k \bowtie mk \bowtie mc$ |
| true Y | 4 | 1,588 | 148.6K |
| est. \hat{Y} | 1 | 8,739 | 104 |
| Q-error q | 4 | 5.50 | 1,428.38 |

| 5-way joins (CARDINALITY only) | | |
|--------------------------------|--|--|
| index ρ | 1 | |
| sub-plan | $cn \bowtie mc \bowtie t \bowtie mk \bowtie k$ | |
| true Y | 4 | |
| est. \hat{Y} | 1 | |
| Q-error q | 4 | |

| Plan | Join order | $\mathcal{C}(\mathcal{P}, Y)$ | $\mathcal{C}(\mathcal{P}, \hat{Y})$ |
|---------------------|--|-------------------------------|-------------------------------------|
| \mathcal{P}_{opt} | $cn \bowtie mc \bowtie t \bowtie mk \bowtie k$ | 2,364 | 10.7K |
| \mathcal{P}_{pg} | $k \bowtie mk \bowtie t \bowtie mc \bowtie cn$ | 232.2K | 144 |

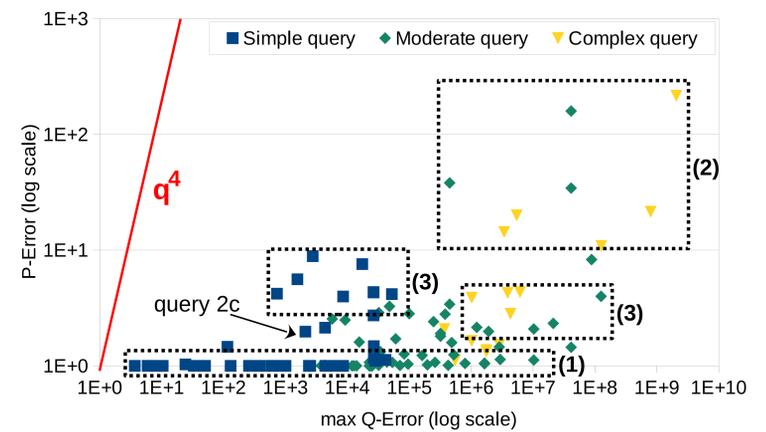
Query plan enumeration over the search space corresponding to JOB query 2c.

2 Q-error

$$q_i = \max \left(\frac{\hat{Y}_i}{Y_i}, \frac{Y_i}{\hat{Y}_i} \right) \quad (1) \quad \frac{\mathcal{C}(\mathcal{P}_{pg}, Y)}{\mathcal{C}(\mathcal{P}_{opt}, Y)} \leq q^4 \quad (2)$$

where Y_i and \hat{Y}_i are true and estimated cardinality of a single sub-plan. $q = \max_{i \in X} \{q_i\}$ and X is the set of all sub-plans. The cost ratio is called *P-error*.

The bound states that, given the estimated and true cardinalities of a query, the cost ratio of any query plan and the optimal query plan is at most q^4 .



P-error and Q-error are computed for all 113 JOB queries. Queries complexity: 45 Simple (4-9 joins), 53 Moderate (10-19 joins), and 15 Complex (20-28 joins).

Observations:

- ▶ **loose as a bound** — large Q-error and small P-error
- ▶ **no observable relationship** — between Q-error and P-error
- ▶ **reversed relationship** — smaller Q-error with larger P-error and vice versa

3 L1-error

Spearman's footrule (a.k.a. L1-distance):

$$L1^k(\rho, \hat{\rho}) = \sum_i^d |\rho(i) - \hat{\rho}(i)|$$

where $\rho(i)$ and $\hat{\rho}(i)$ are the indexes of i -th sub-plan in the position vectors. In the case of identical sub-plan arrangements, $L1^k(\rho, \hat{\rho}) = 0$.

Our Objectives – Weighted L1-error:

- ▶ Significantly over and underestimating cardinality should be associated with greater penalties. Conversely, mispositioning sub-plans with similar cardinalities in the position vectors should carry fewer and relatively similar penalties.
- ▶ Cardinality misestimations that occur early in the position vector should attract greater penalties. This is particularly beneficial for plan search algorithms, which are more likely to choose a sub-plan from the first half of the position vector.

| 2-way join (CARDINALITY only) | | | | | |
|-------------------------------|-----|--------|-------|--------|--------|
| ρ | 1 | 2 | 3 | 4 | 5 |
| $\hat{\rho}$ | 2 | 1 | 3 | 4 | 5 |
| Swap cost | 1.0 | 107.84 | 62.36 | 1.73 | 7.71 |
| Monotonic weight | 1.0 | 108.84 | 171.2 | 172.93 | 180.64 |

| 3-way join (CARDINALITY only) | | | | | |
|-------------------------------|-----|------|-------|-------|--------|
| ρ | 1 | 2 | 3 | 4 | 5 |
| $\hat{\rho}$ | 3 | 4 | 1 | 2 | 5 |
| Swap cost | 1.0 | 4.09 | 26.35 | 3.55 | 234.69 |
| Monotonic weight | 1.0 | 5.09 | 31.44 | 34.99 | 269.68 |

| 4-way join (CARDINALITY only) | | | |
|-------------------------------|-----|-------|--------|
| ρ | 1 | 2 | 3 |
| $\hat{\rho}$ | 1 | 3 | 2 |
| Swap cost | 1.0 | 397.0 | 93.55 |
| Monotonic weight | 1.0 | 398.0 | 491.55 |

| Impact weight, W (2-way join) | | | | | |
|-------------------------------|-----|--------|----------|-----------|-----------|
| | 1 | 2 | 3 | 4 | 5 |
| 1 | 1.0 | 107.84 | 6,724.56 | 11,659.61 | 89,854.74 |
| 2 | | 1.0 | 62.36 | 108.12 | 833.26 |
| 3 | | | 1.0 | 1.73 | 13.36 |
| 4 | | | | 1.0 | 7.71 |
| 5 | | | | | 1.0 |

| Impact weight, W (3-way join) | | | | | |
|-------------------------------|-----|------|--------|--------|-----------|
| | 1 | 2 | 3 | 4 | 5 |
| 1 | 1.0 | 4.09 | 107.84 | 382.87 | 89,854.74 |
| 2 | | 1.0 | 26.35 | 93.55 | 21,954.43 |
| 3 | | | 1.0 | 3.55 | 833.26 |
| 4 | | | | 1.0 | 234.69 |
| 5 | | | | | 1.0 |

| Impact weight, W (4-way join) | | | |
|-------------------------------|-----|-------|----------|
| | 1 | 2 | 3 |
| 1 | 1.0 | 397.0 | 37,138.0 |
| 2 | | 1.0 | 93.55 |
| 3 | | | 1.0 |

Sub-plan weights used by the plan enumeration algorithms for JOB query 2c.

4 Experiments - L1-error classifier accuracy on test data using PostgreSQL cardinality estimates

| | Predicted | | True |
|---|-----------------------|--------------------|-----------------------|-----------------------|--------------------|-----------------------|-----------------------|--------------------|-----------------------|-----------------------|--------------------|-----------------------|
| | Positive (suboptimal) | Negative (optimal) | | Positive (suboptimal) | Negative (optimal) | | Positive (suboptimal) | Negative (optimal) | | Positive (suboptimal) | Negative (optimal) | |
| DSB benchmark, Exhaustive enumeration, 1152 train and 288 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |
| DSB benchmark, Greedy enumeration, 1152 train and 288 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |
| JCCH benchmark, Exhaustive enumeration, 408 train and 103 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |
| JCCH benchmark, Greedy enumeration, 408 train and 103 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |
| JOB benchmark, Exhaustive enumeration, 79 train and 34 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |
| JOB benchmark, Greedy enumeration, 79 train and 34 test queries. | TP = 124 43.06% | FP = 15 5.21% | Positive (suboptimal) | TP = 105 36.46% | FP = 18 6.25% | Positive (suboptimal) | TP = 28 27.18% | FP = 0 0.00% | Positive (suboptimal) | TP = 14 13.59% | FP = 0 0.00% | Positive (suboptimal) |
| | FN = 21 7.29% | TN = 128 44.44% | | FN = 29 10.07% | TN = 136 47.22% | | FN = 2 1.94% | TN = 73 70.87% | | FN = 10 9.71% | TN = 79 76.70% | |